

1 Utför följande konverteringar av positiva tal.

a)  $67.24_8$  till decimal form

$$67.24_8 = 6 \cdot 8^1 + 7 \cdot 8^0 + 2 \cdot 8^{-1} + 4 \cdot 8^{-2} = 55.3125$$

b)  $9714_{10}$  till hexadecimal form

|                | Kvot | Rest   |
|----------------|------|--------|
| $9714 \div 16$ | 607  | 2      |
| $607 \div 16$  | 37   | 15 (F) |
| $37 \div 16$   | 2    | 5      |
| $2 \div 16$    | 0    | 2      |

$$9714_{10} = 25F2_{16}$$

2. Beskriv hur man detekterar overflow i 2-komplement addition

"Overflow" inträffar då operanderna har samma tecken och summans tecken skiljer sig från operandernas tecken.

3. Visa följande likheter med hjälp av räknelagar

a)  $xy(xy + \bar{x}y + wxy) = xy$

$$\text{V.L} = xy(xy + \bar{x}y + wxy)$$

med absorptionslagarna

$$= xy$$

b)  $wx + \bar{w}y + xyz = wx + \bar{w}y$

$$\text{V.L} = wx + \bar{w}y + xyz =$$

$$= wx + \bar{w}y + xy + xyz \quad (\text{concensus})$$

$$= wx + \bar{w}y + xy \quad (\text{absorptionslag})$$

$$= wx + \bar{w}y \quad (\text{concensus})$$

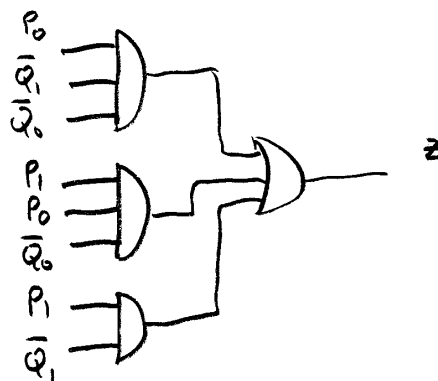
4. Konstruera en jämförar-krets som tar in P och Q och ger ut  $z = 1$  om  $P > Q$

| $P_1$ | $P_0$ | $Q_1$ | $Q_0$ | $z$ |
|-------|-------|-------|-------|-----|
| 0     | 0     | 0     | 0     | 0   |
| 0     | 0     | 0     | 1     | 0   |
| 0     | 0     | 1     | 0     | 0   |
| 0     | 0     | 1     | 1     | 0   |
| 0     | 1     | 0     | 0     | 1   |
| 0     | 1     | 0     | 1     | 0   |
| 0     | 1     | 1     | 0     | 0   |
| 0     | 1     | 1     | 1     | 0   |
| 1     | 0     | 0     | 0     | 1   |
| 1     | 0     | 0     | 1     | 0   |
| 1     | 0     | 1     | 0     | 0   |
| 1     | 0     | 1     | 1     | 0   |
| 1     | 1     | 0     | 0     | 1   |
| 1     | 1     | 0     | 1     | 0   |
| 1     | 1     | 1     | 0     | 1   |
| 1     | 1     | 1     | 1     | 0   |

Karnaugh diagram:

|           |    | $Q_1 Q_0$ |    |    |    |
|-----------|----|-----------|----|----|----|
|           |    | 00        | 01 | 11 | 10 |
| $P_1 P_0$ | 00 | 0         | 0  | 0  | 0  |
|           | 01 | 0         | 0  | 0  | 0  |
|           | 11 | 1         | 1  | 0  | 0  |
|           | 10 | 1         | 1  | 0  | 0  |

$$z = P_1 \bar{Q}_1 + P_0 \bar{Q}_1 \bar{Q}_0 + P_1 P_0 \bar{Q}_0$$



5. Ta fram kombinatoriska nät för utgångarna där de gemensamma termerna utnyttjas så långt det är möjligt.

| $x_3$ | $x_2$ | $x_1$ | $u_2$ | $u_1$ |
|-------|-------|-------|-------|-------|
| 0     | 0     | 0     | 0     | 0     |
| 0     | 0     | 1     | 0     | 1     |
| 0     | 1     | 0     | 1     | 1     |
| 0     | 1     | 1     | 0     | 1     |
| 1     | 0     | 0     | 0     | 1     |
| 1     | 0     | 1     | 1     | 1     |
| 1     | 1     | 0     | 0     | 1     |
| 1     | 1     | 1     | 0     | 0     |

Karnaugh diagram:

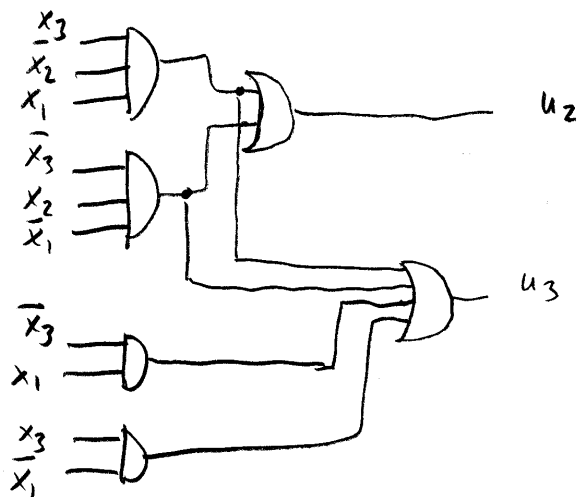
|       |   | $x_2 x_1$ |    |    |    |
|-------|---|-----------|----|----|----|
|       |   | 00        | 01 | 11 | 10 |
| $x_3$ | 0 | 0         | 0  | 0  | 1  |
|       | 1 | 0         | 1  | 0  | 0  |

$u_2$

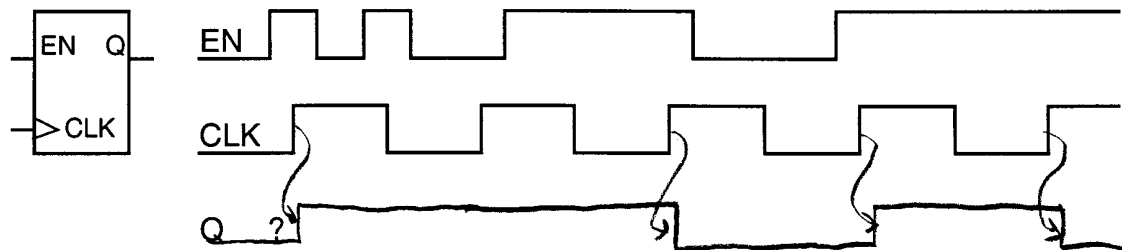
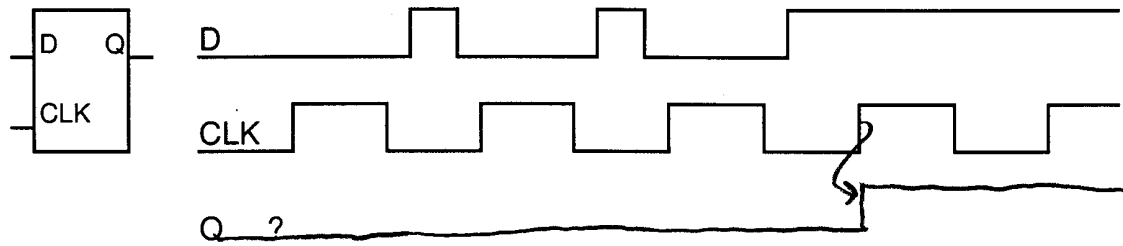
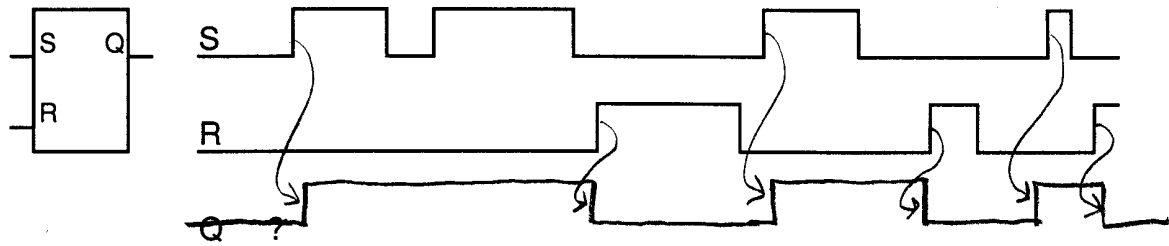
|       |   | $x_2 x_1$ |    |    |    |
|-------|---|-----------|----|----|----|
|       |   | 00        | 01 | 11 | 10 |
| $x_3$ | 0 | 0         | 1  | 1  | 1  |
|       | 1 | 1         | 1  | 0  | 1  |

$u_1$

$$u_2 = x_3 \bar{x}_2 x_1 + \bar{x}_3 x_2 \bar{x}_1; \quad u_1 = x_3 \bar{x}_2 x_1 + \bar{x}_3 x_2 \bar{x}_1 + \bar{x}_3 x_1 + x_3 \bar{x}_1$$



6. Rita vågformen för utgången  $Q$  för vardera av följande tre latchar/vippor (3 p)



7. Ta fram tillståndstabell och tillståndsgraf.

Booleska uttryck:

$$J_2 = \overline{x} \overline{q_1} \quad K_2 = 1$$

$$J_1 = 1 \quad K_1 = q_2 \overline{x}$$

$$u = \overline{q_2} q_1$$

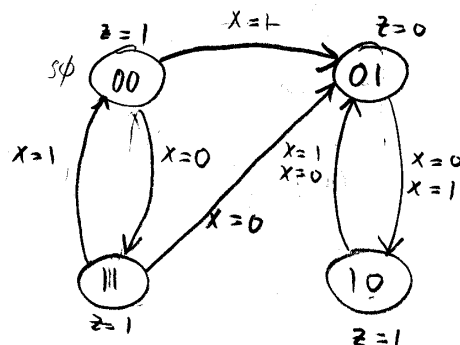
J och K värden

|           | $x=0$             | $x=1$             |
|-----------|-------------------|-------------------|
| 00        | 1 1 1 1           | 0 1 1 1           |
| 01        | 1 1 1 1           | 1 1 1 1           |
| 10        | 1 1 1 0           | 0 1 1 1           |
| 11        | 1 1 1 0           | 1 1 1 1           |
| $q_2 q_1$ | $J_2 K_2 J_1 K_1$ | $J_2 K_2 J_1 K_1$ |

Tillståndstabell

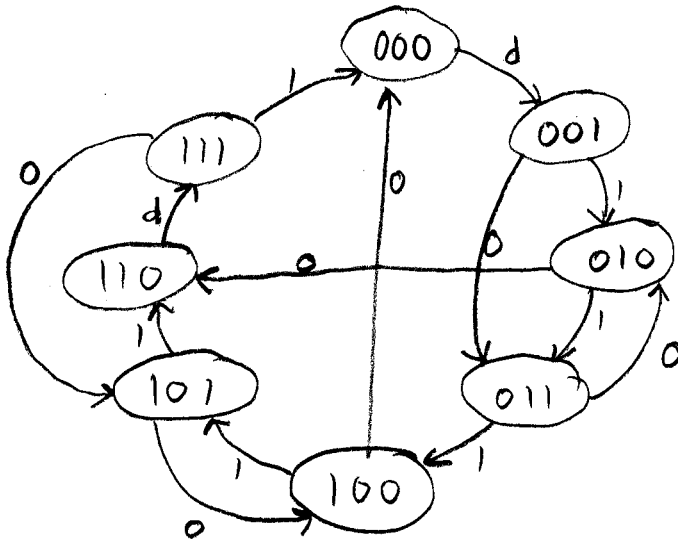
|           | $x=0$             | $x=1$   |
|-----------|-------------------|---------|
| 00        | 1 1 (1)           | 0 1 (1) |
| 01        | 1 0 (0)           | 1 0 (0) |
| 10        | 0 1 (1)           | 0 1 (1) |
| 11        | 0 1 (1)           | 0 0 (1) |
| $q_2 q_1$ | $q_2^+ q_1^+ (u)$ |         |

Tillståndsgraf



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Tillståndsgraf:



Tillståndstabell

| $b/\bar{q}$ | $Q_2$ | $Q_1$ | $Q_0$ | $Q_2^+$ | $Q_1^+$ | $Q_0^+$ |
|-------------|-------|-------|-------|---------|---------|---------|
| 0           | 0     | 0     | 0     | 0       | 0       | 1       |
| 0           | 0     | 0     | 1     | 0       | 1       | 0       |
| 0           | 0     | 1     | 0     | 1       | 1       | 0       |
| 0           | 0     | 1     | 1     | 0       | 0       | 0       |
| 0           | 1     | 0     | 0     | 0       | 0       | 0       |
| 0           | 1     | 0     | 1     | 0       | 0       | 0       |
| 0           | 1     | 1     | 0     | 1       | 0       | 1       |
| 0           | 1     | 1     | 1     | 0       | 1       | 0       |
| 1           | 0     | 0     | 0     | 0       | 0       | 1       |
| 1           | 0     | 0     | 1     | 0       | 1       | 0       |
| 1           | 0     | 1     | 0     | 1       | 1       | 0       |
| 1           | 0     | 1     | 1     | 0       | 0       | 0       |
| 1           | 1     | 0     | 0     | 0       | 0       | 1       |
| 1           | 1     | 0     | 1     | 0       | 1       | 0       |
| 1           | 1     | 1     | 0     | 1       | 0       | 1       |
| 1           | 1     | 1     | 1     | 0       | 1       | 0       |

for 1s ~~8~~ 8

$Q_1, Q_0$

|                 | 00 | 01 | 11 | 10 |
|-----------------|----|----|----|----|
| $b/g \cdot Q_2$ | 0  | 0  | 0  | 1  |
| 0               | 0  | 0  | 0  | 1  |
| 1               | 0  | 0  | 1  | 0  |
| 1               | 0  | 0  | 1  | 0  |

$Q_2^+$

$Q_1, Q_0$

|                 | 00 | 01 | 11 | 10 |
|-----------------|----|----|----|----|
| $b/g \cdot Q_2$ | 0  | 0  | 0  | 1  |
| 0               | 0  | 0  | 0  | 1  |
| 1               | 0  | 0  | 1  | 0  |
| 1               | 0  | 0  | 1  | 0  |

$Q_1^+$

$Q_1, Q_0$

|                 | 00 | 01 | 11 | 10 |
|-----------------|----|----|----|----|
| $b/g \cdot Q_2$ | 0  | 0  | 0  | 1  |
| 0               | 0  | 0  | 0  | 1  |
| 1               | 0  | 0  | 1  | 0  |
| 1               | 0  | 0  | 1  | 0  |

$Q_0^+$

Kar  $D = Q^+$

$$D_2 = \overline{b/g} \cdot Q_1 \cdot \overline{Q_0} + Q_2 \cdot Q_1 \cdot \overline{Q_0} + \overline{b/g} \cdot Q_2 \cdot \overline{Q_1} + \overline{b/g} \cdot Q_2 \cdot Q_0 + \overline{b/g} \cdot \overline{Q_2} \cdot Q_1 \cdot Q_0$$

$$D_1 = Q_1 \cdot \overline{Q_0} + \overline{b/g} \cdot \overline{Q_1} \cdot Q_0 + \overline{b/g} \cdot \overline{Q_2} \cdot Q_0$$

$$D_0 = \overline{b/g} \cdot \overline{Q_0} + \overline{b/g} \cdot \overline{Q_2} \cdot \overline{Q_1} + \overline{b/g} \cdot Q_2 \cdot Q_1$$

Logikschema:

